

PKC 2016

# Identity-based Hierarchical Key-insulated Encryption without Random Oracles

Yohei Watanabe<sup>1,3</sup>

Junji Shikata<sup>1,2</sup>

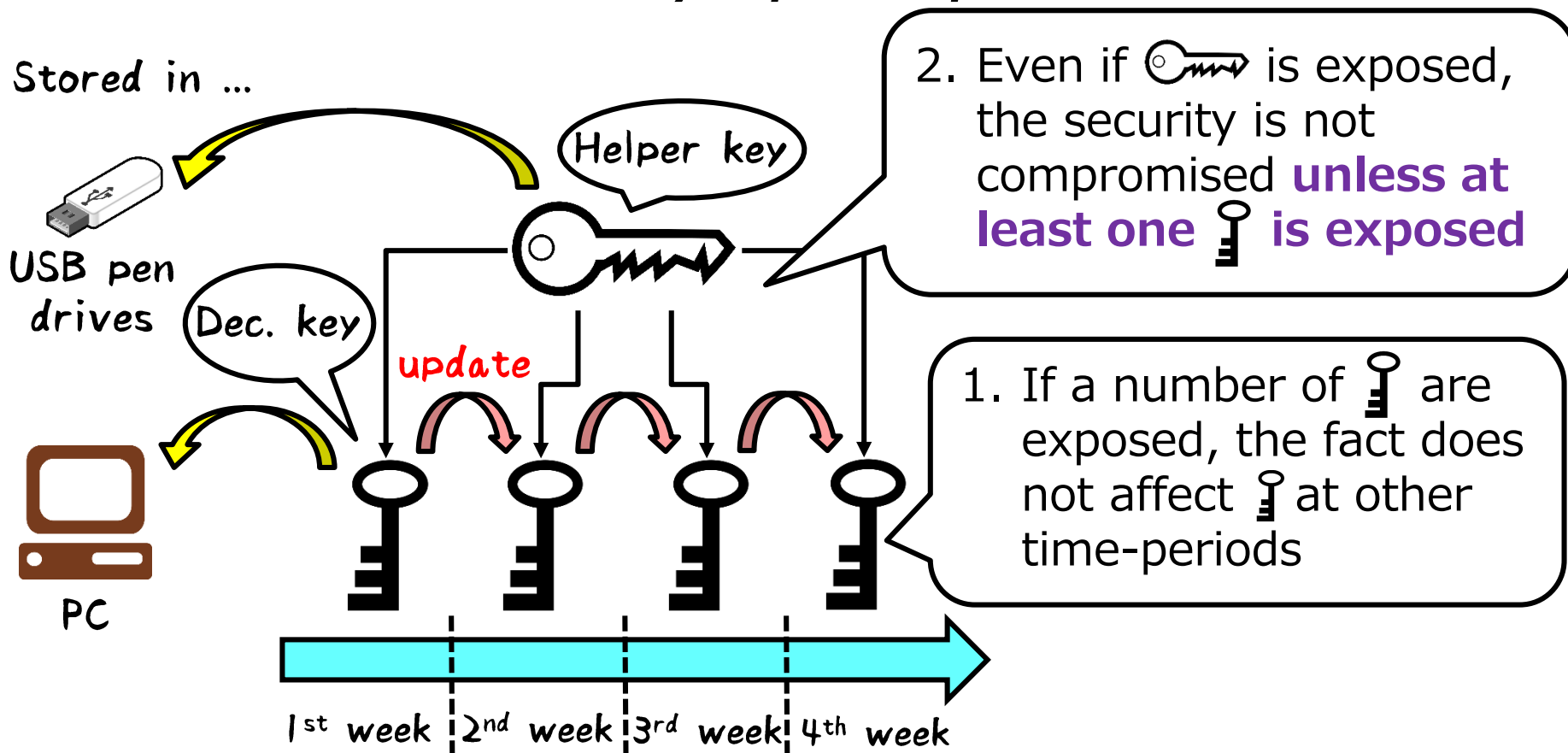
1 Graduate School of Environment and Information Sciences,  
YNU, Japan

2 Institute of Advanced Sciences, YNU, Japan

3. ITRI, AIST, Japan

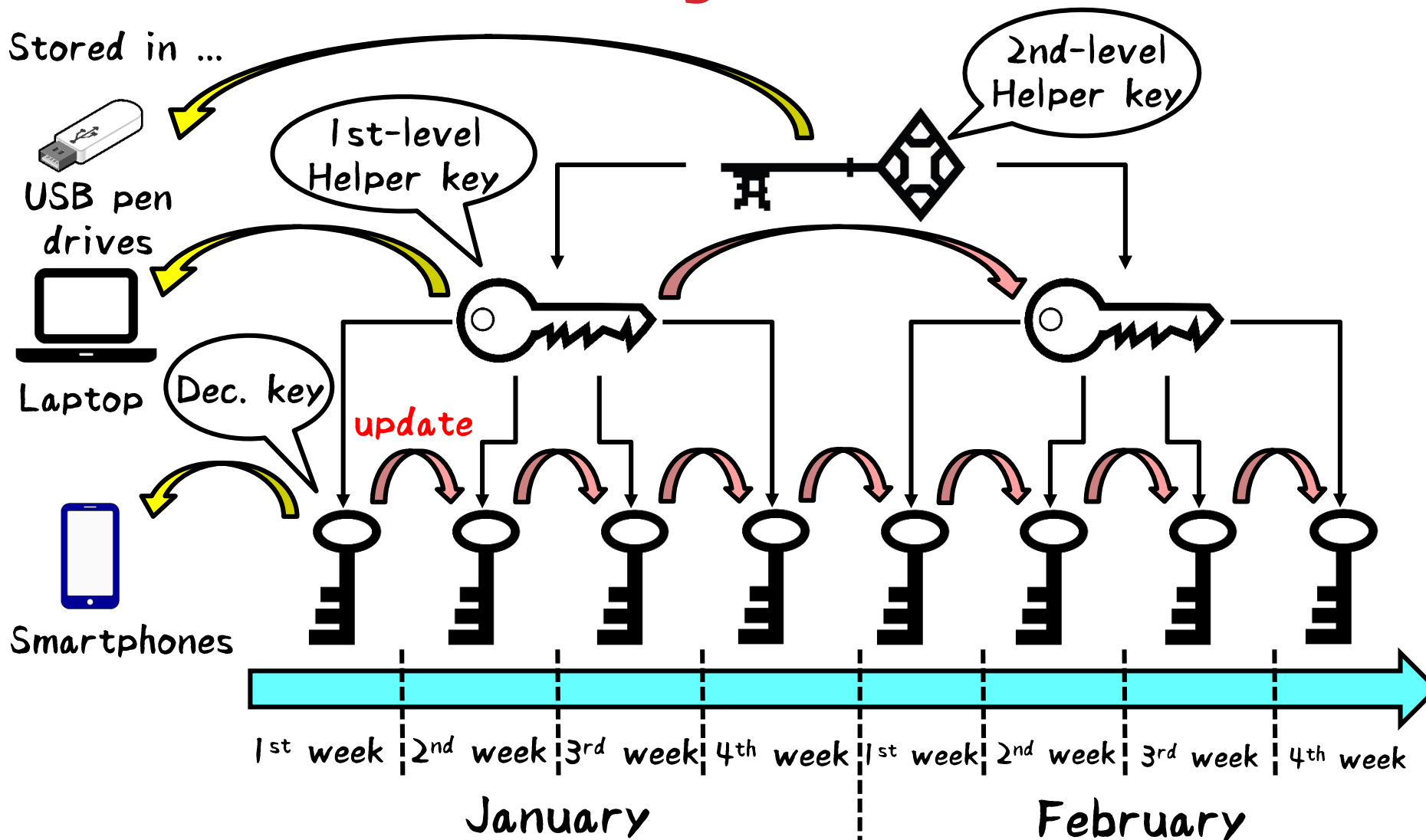
# Key Insulation [DKXY02]

## ◆ One of solutions to *key exposure problem*



The scheme is  $\left\{ \begin{array}{l} \text{secure if it satisfies 1} \\ \text{strongly secure if it satisfies both 1 and 2} \end{array} \right.$  **2**

# Hierarchical Key Insulation [HHSI05]



There seem to be various practical applications !

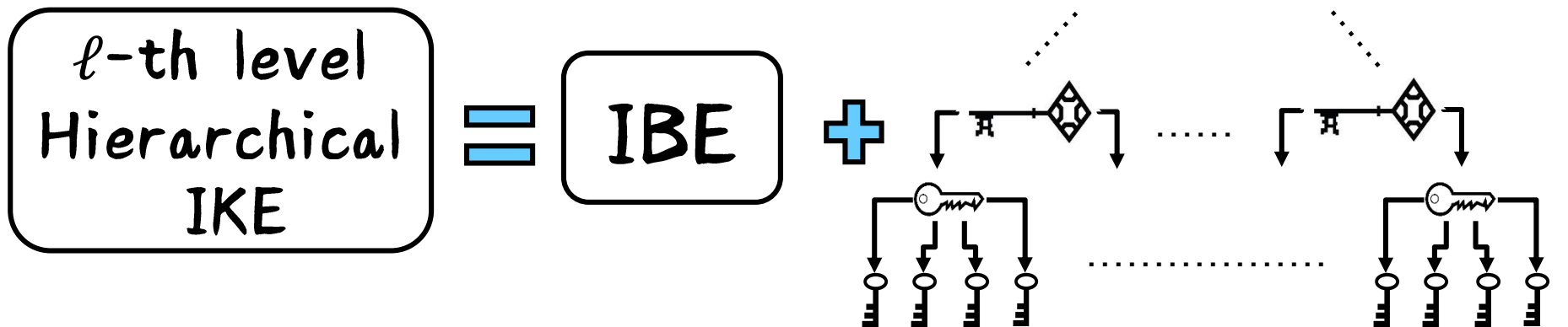
# Identity-based Hierarchical Key-insulated Encryption [HHS105]

## ◆ Abbreviated to “hierarchical IKE”

☺ Identity-based encryption (IBE) with hierarchical key insulation

☹ NOT hierarchical IBE (HIBE) with key insulation

## Intuition:



## ◆ First proposed by Hanaoka et al. at ASIACRYPT 2005 [HHS105]

◆ In the random oracle model (ROM)

However, NO known hierarchical IKE schemes w/o ROM !

# Our Contribution

We propose an  $\ell$ -level hierarchical IKE scheme that achieves:

- (1) **Strong security in the standard model from simple assumptions**
  - ✓ Using asymmetric pairing
  - ✓ From Symmetric eXternal Diffie-Hellman (SXDH) assumption
  - ✓ Based on Jutla-Roy HIBE [JR13] and its variant [RS14]
- (2) **Space efficiency (any parameters do not depend on ID-space sizes)**
  - ✓ Constant-size parameters when the hierarchy is one (i.e.  $\ell = 1$ )
    - Public parameters of the existing scheme [WLC+08] depend on ID-space sizes due to the underlying Waters IBE [wat05]

Why is achieving (1) and (2) challenging? (more on this later)

- Hierarchical IKE from any HIBE does not satisfy strong security
- Proof technique of Waters dual-system IBE [Wat09] does not work well

# Type-3 Pairing and SXDH Assumption

## Type-3 Pairing (asymmetric pairing)

- ✓  $e: \mathbb{G}_1 \times \mathbb{G}_2 \rightarrow \mathbb{G}_T$
- ✓ No efficiently computable isomorphisms between  $\mathbb{G}_1$  and  $\mathbb{G}_2$  are known

## SXDH Assumption [BBS04]

- ✓ Decisional Diffie–Hellman (DDH) assumptions hold in  $\mathbb{G}_1$  and  $\mathbb{G}_2$ , respectively
- ✓ Advantage of  $\mathcal{A}$  in the DDH $_i$  game ( $i \in \{1, 2\}$ ) is defined by:

$$Adv(\lambda) := Pr \left[ b' = b \mid \begin{array}{l} D := (p, \mathbb{G}_1, \mathbb{G}_2, \mathbb{G}_T, g_1, g_2, e) \leftarrow \mathcal{G} \\ c_1, c_2 \leftarrow \mathbb{Z}_p, b \leftarrow \{0, 1\} \\ \text{if } b = 0 \text{ then } T := g_i^{c_1 c_2} \text{ else } T \leftarrow \mathbb{G}_i \\ b' \leftarrow \mathcal{A}(D, g_i^{c_1}, g_i^{c_2}, T) \end{array} \right].$$

# Time-period Map Function [HHS105]

✓ Functions for “several kinds of time-periods”  $\mathcal{T}_0, \dots, \mathcal{T}_{\ell-1}$

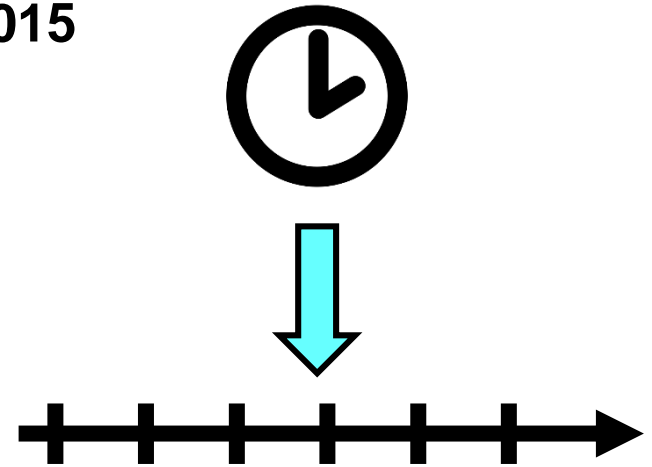
Example:  $\ell = 4$ , time = 9:59 / 7th / Oct. / 2015

$$\mathcal{T}_0(\text{time}) = t_0^{(19)} = \text{1st} - \text{15th} / \text{Oct.} / \text{2015},$$

$$\mathcal{T}_1(\text{time}) = t_1^{(10)} = \text{Oct.} / \text{2015},$$

$$\mathcal{T}_2(\text{time}) = t_2^{(5)} = \text{Set.} - \text{Oct.} / \text{2015},$$

$$\mathcal{T}_3(\text{time}) = t_3^{(2)} = \text{Jul.} - \text{Dec.} / \text{2015}$$



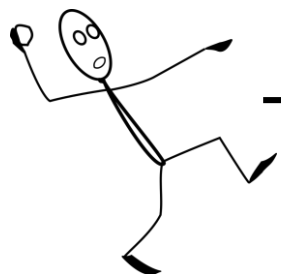
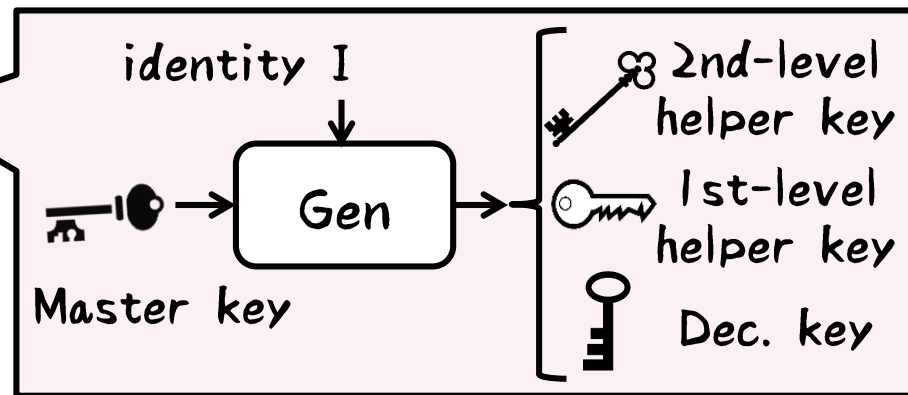
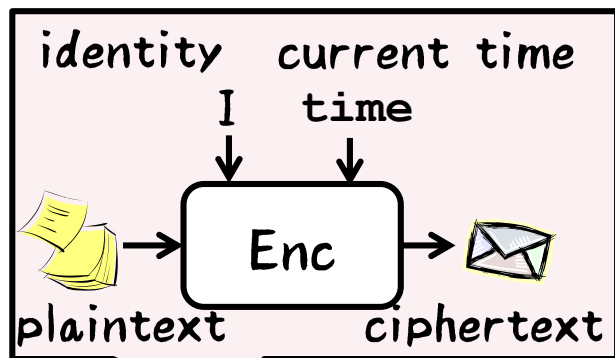
Jan. Feb. Mar. Apr. May Jun. Jul. Aug. Sep. Oct. Nov. Dec.

$\mathcal{T}_3$	$t_3^{(1)}$										$t_3^{(2)}$													
$\mathcal{T}_2$	$t_2^{(1)}$				$t_2^{(2)}$				$t_2^{(3)}$				$t_2^{(4)}$				$t_2^{(5)}$				$t_2^{(6)}$			
$\mathcal{T}_1$	$t_1^{(1)}$	$t_1^{(2)}$	$t_1^{(3)}$	$t_1^{(4)}$	$t_1^{(5)}$	$t_1^{(6)}$	$t_1^{(7)}$	$t_1^{(8)}$	$t_1^{(9)}$	$t_1^{(10)}$	$t_1^{(11)}$	$t_1^{(12)}$	$t_1^{(13)}$	$t_1^{(14)}$	$t_1^{(15)}$	$t_1^{(16)}$	$t_1^{(17)}$	$t_1^{(18)}$	$t_1^{(19)}$	$t_1^{(20)}$	$t_1^{(21)}$	$t_1^{(22)}$	$t_1^{(23)}$	$t_1^{(24)}$
$\mathcal{T}_0$	$t_0^{(1)}$	$t_0^{(2)}$	$t_0^{(3)}$	$t_0^{(4)}$	$t_0^{(5)}$	$t_0^{(6)}$	$t_0^{(7)}$	$t_0^{(8)}$	$t_0^{(9)}$	$t_0^{(10)}$	$t_0^{(11)}$	$t_0^{(12)}$	$t_0^{(13)}$	$t_0^{(14)}$	$t_0^{(15)}$	$t_0^{(16)}$	$t_0^{(17)}$	$t_0^{(18)}$	$t_0^{(19)}$	$t_0^{(20)}$	$t_0^{(21)}$	$t_0^{(22)}$	$t_0^{(23)}$	$t_0^{(24)}$

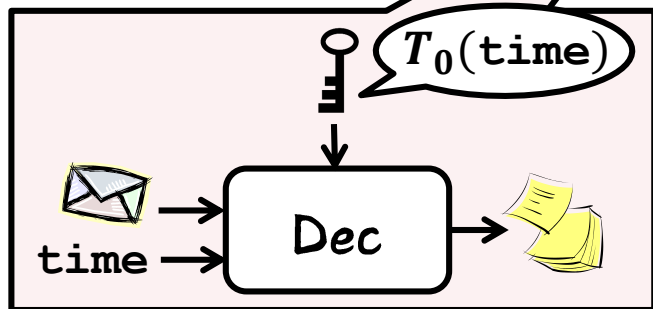
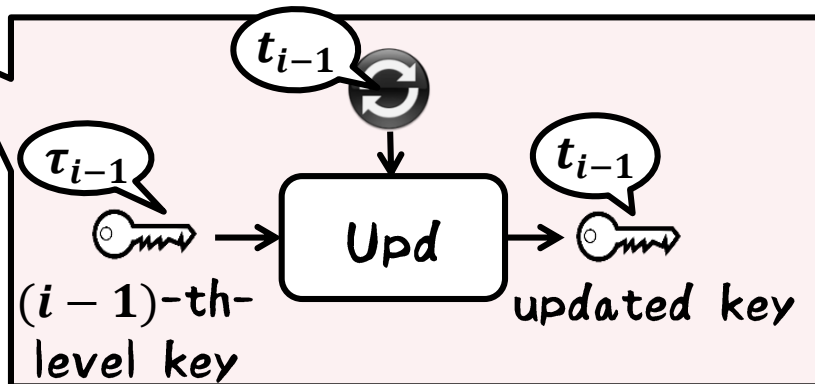
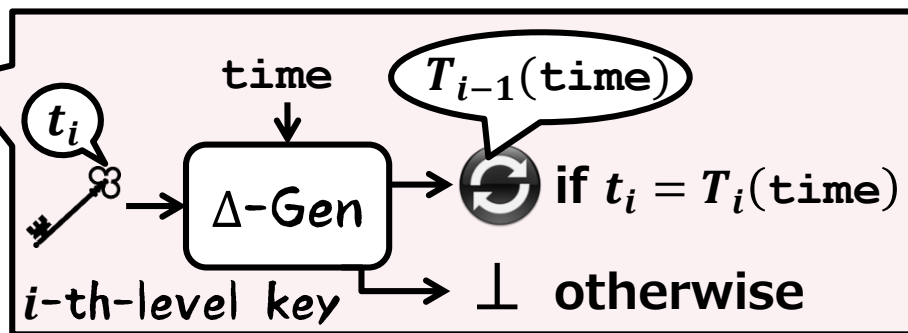
↑  
time

# Hierarchical IKE: Model

Example:  $\ell = 2$



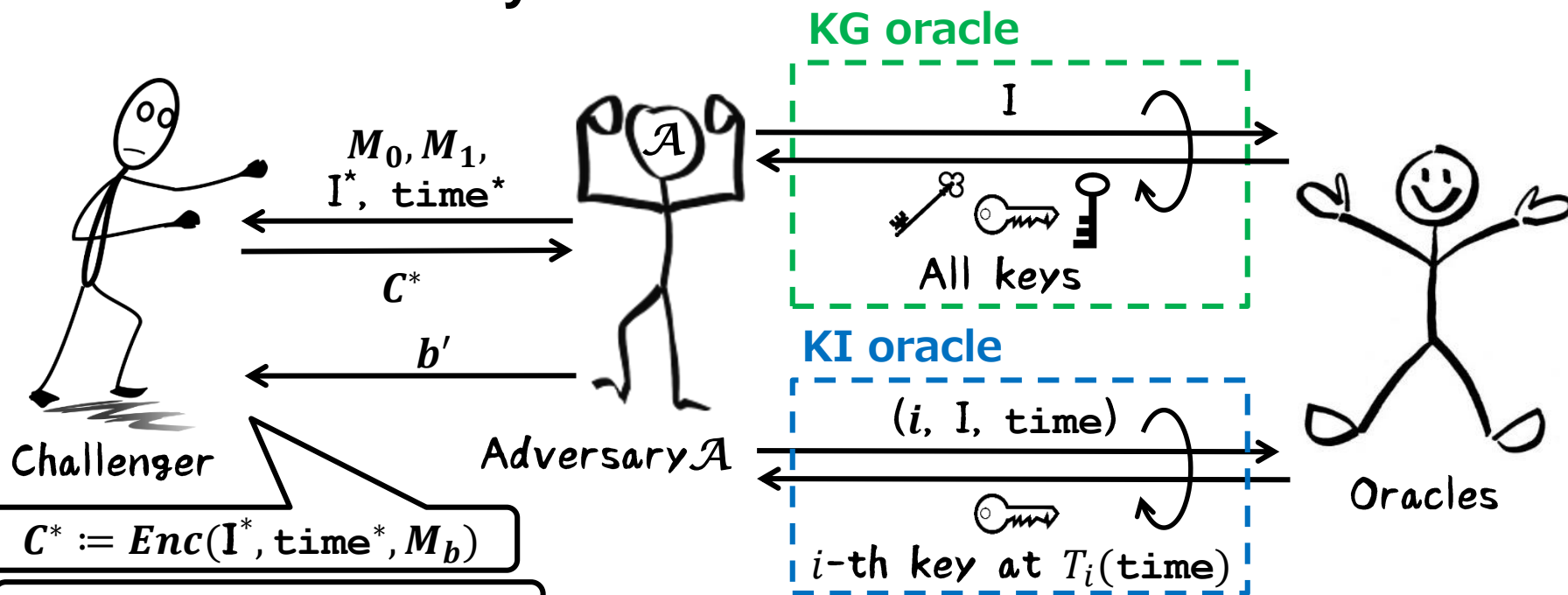
$\langle \text{ciphertext}, \text{time} \rangle$





# Hierarchical IKE: Security

IND-KE-CPA security:



## Limitation of KI oracle

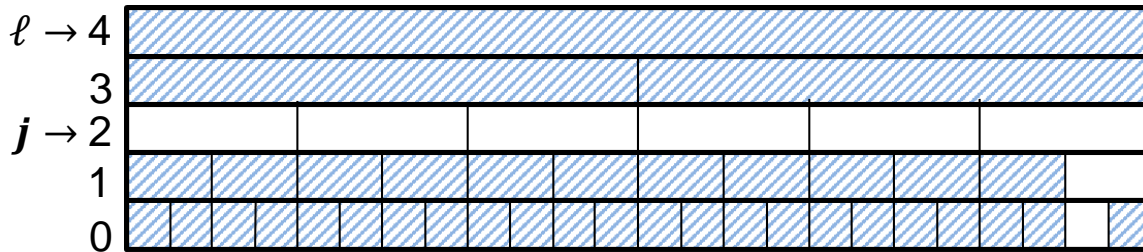
$\mathcal{A}$  can issue any queries if there exists

at least one special level

$j \in \{0, \dots, \ell\}$

→ include strong security

Hierarchy

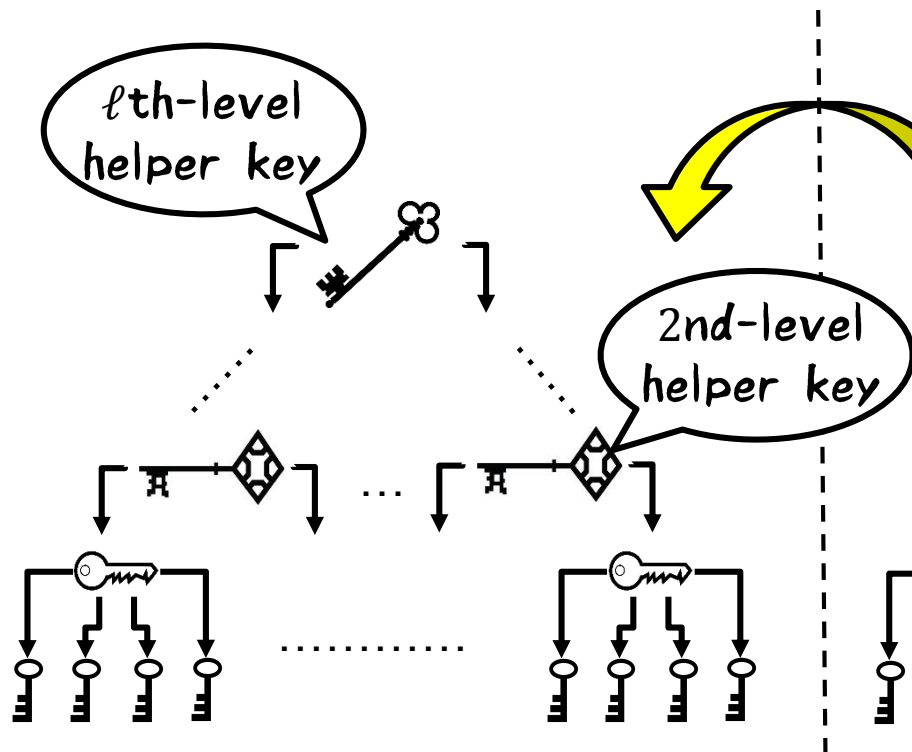


▨: Keys for  $I^*$  that  $\mathcal{A}$  can obtain

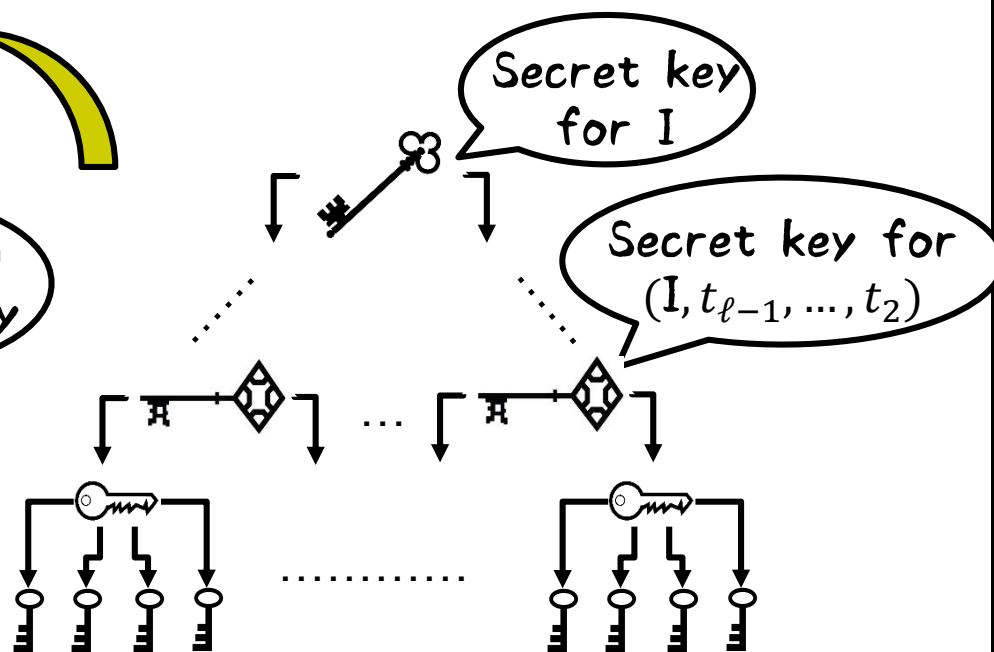
↑ time\*

# Why Hierarchical IKE from HIBE is Insufficient

$\ell$ -level Hierarchical IKE



$(\ell + 1)$ -level HIBE



If secret key for  $I$  is leaked, all other secret keys can be generated

→ the resulting scheme does not meet *strong* security

→ does not meet IND-KE-CPA security !

# Why Waters' Technique Does Not Work

Waters dual system IBE [Wat09]

➤ Ciphertext  $ct$  contains  $tag_C$  and secret key  $sk_I$  contains  $tag_K$

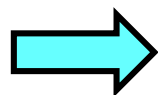
**Important proof technique:**

Some pairwise independent function is embedded into the public parameter for cancelling values

- It raises  $tag_C = tag_K$  for the same identity  $I$
- However, **the proof works well** since it is enough to generate
  - Only  $tag_K$  for all identities  $I \neq I^*$
  - Only  $tag_C$  for the target identity  $I^*$

On the other hand, in (hierarchical) IKE,

$\mathcal{A}$  can get **secret keys for  $I^*$  (i.e.  $tag_K$ )** as well as for  $I \neq I^*$



**Waters' technique cannot seem to be applied !**

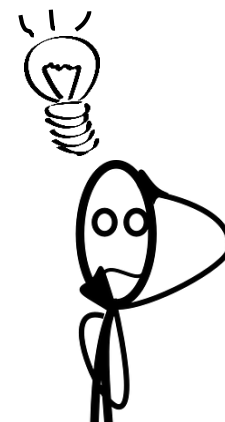
# Why Jutla–Roy HIBE?

We can avoid such a collision problem!

✓  $sk_I$  does not contain any tag, though  $ct$  contains  $tag$

## ◆ Jutla–Roy HIBE [JR13] and its variant [RS14]

- ◆ Constant-size IBE (when  $\ell = 1$ )
- ◆ IND-ID-CPA security under the SXDH assumption
- ◆ Constant-size lowest-level key unlike [Wat09,LW11]
  - It leads to constant-size decryption key



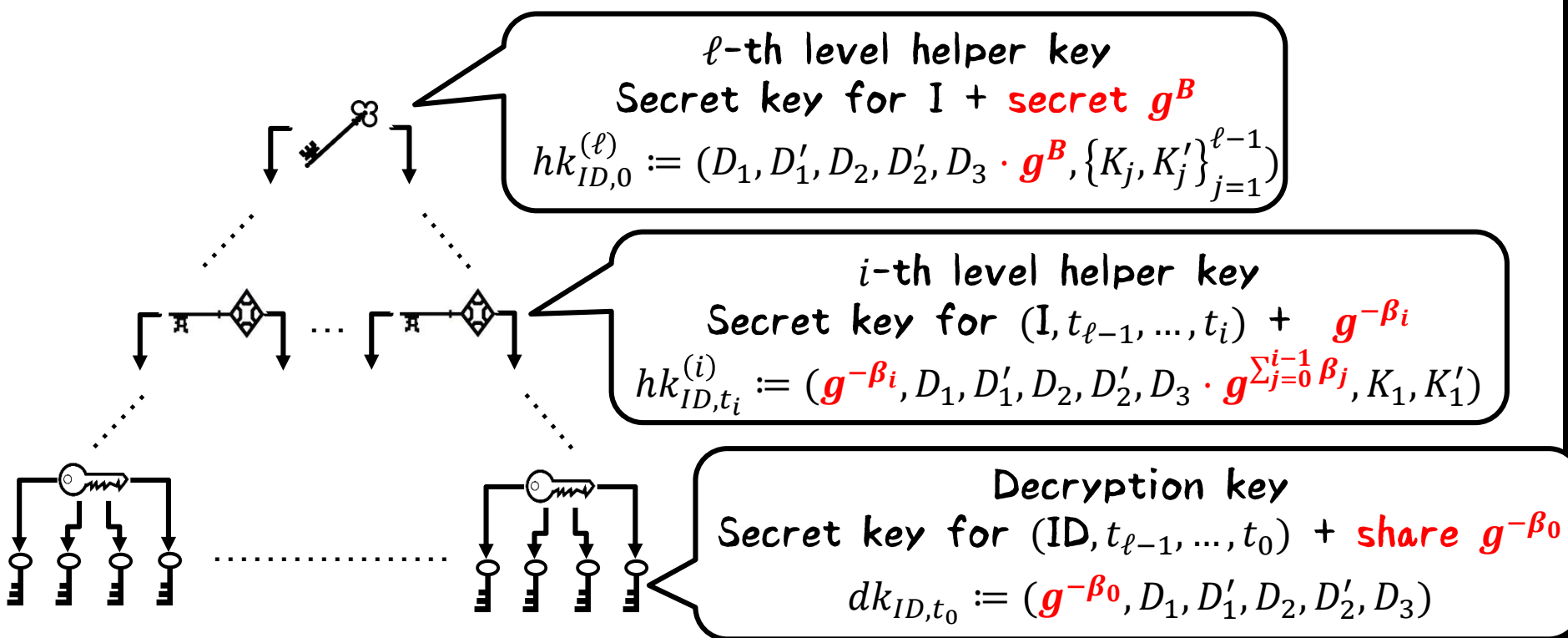
### Remark

There might be other constant-size IBE schemes that can avoid the collision problem

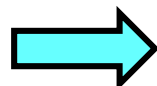
# Basic Idea of Our Construction

Specific  $(\ell + 1)$ -level HIBE (  $(\ell + 1)$ -level Jutla–Roy HIBE ) +

$(\ell, \ell)$ -secret sharing: **secret  $B$  and shares  $\beta_i$  ( $0 \leq i \leq \ell - 1$ ) s.t.  $B = \sum_{i=0}^{\ell-1} \beta_i$**



**All  $\beta_i$  are needed to generate correct decryption key  $(D_1, D'_1, D_2, D'_2, D_3)$**



**Adversary cannot generate decryption key for  $I^*$  at time\* !**

# Encryption and Decryption Procedure

$Enc(mp_k, I, \mathbf{time}, M)$ :

$$mp_k := (z, g_1, g_1^\alpha, \{u_{1,j}\}_{j=0}^\ell, w_1, h_1, \dots)$$

Choose  $s, tag \leftarrow \mathbb{Z}_p$ . Compute

$$C_0 := Mz^s, C_1 := g_1^s, C_2 := (g_1^\alpha)^s, C_3 := \left( \prod_{j=0}^{\ell-1} (u_{1,j}^{t_j}) u_{1,\ell}^I w_1^{tag} h_1 \right)^s,$$

where  $t_j := T_j(\mathbf{time})$  ( $0 \leq j \leq \ell - 1$ ). Output  $C := (C_0, C_1, C_2, C_3, tag)$ .

$Dec(dk_{I,t_0}, \langle C, \mathbf{time} \rangle)$ :

$$dk_{I,t_0} := (R_0, D_1, D'_1, D_2, D'_2, D_3)$$

$$M = \frac{C_0 \cdot e(C_3, D_3)}{e(C_1, D_1^{tag} D'_1) e(C_2, D_2^{tag} D'_2)}.$$

# Parameter Evaluation and Comparison

# $pp$	# $dk$	# $hk_i$	# $C$	Enc. cost	Dec. cost
$(3\ell + 13) \mathbb{G} $	$6 \mathbb{G} $	$(2i + 6) \mathbb{G} $	$4 \mathbb{G}  +  \mathbb{Z}_p $	$[0,0,\ell + 4,1]$	$[3,0,2,0]$

$|\mathbb{G}|$  : bit-length of a group element in  $\mathbb{G}_1$ ,  $\mathbb{G}_2$ , or  $\mathbb{G}_T$

$|\mathbb{Z}_p|$  : bit-length of an element in  $\mathbb{Z}_p$

# $pp$ , # $dk$ , # $hk_i$ , # $C$ : sizes of public parameter, dec. key,  $i$ -th helper key, and ciphertext

[\*,\*,\*,\*] : [pairing, multi-exp., regular-exp., fix-based-exp.]

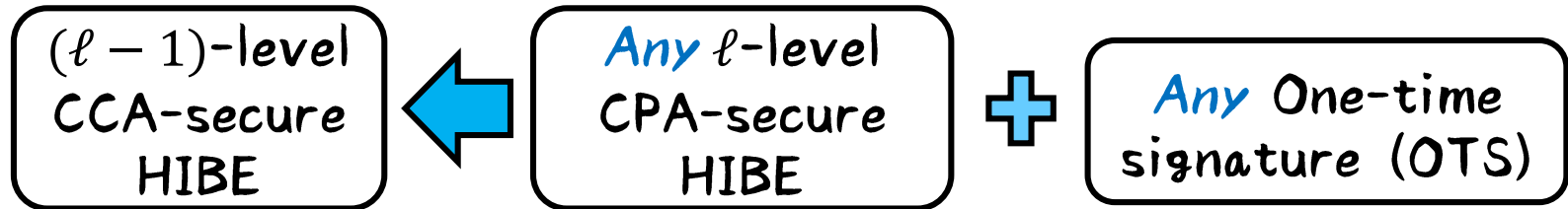
	# $pp$	# $dk$	# $hk$	# $C$	Enc. cost	Dec. cost	Assumption
<b>HHSI05</b> ( $\ell = 1$ )	$2 \mathbb{G} $	$3 \mathbb{G} $	$ \mathbb{G} $	$4 \mathbb{G}  +  r $	$[1,0,2,1]$	$[4,0,2,1]$	<b>CBDH</b> (in ROM)
<b>WLC+08</b> (threshold $t = 1$ )	$(2n + 5) \mathbb{G} $	$4 \mathbb{G} $	$2 \mathbb{G} $	$4 \mathbb{G} $	$[0,1,2,1]$	$[3,0,0,0]$	<b>DBDH</b>
<b>Our scheme</b> ( $\ell = 1$ )	$16 \mathbb{G} $	$6 \mathbb{G} $	$7 \mathbb{G} $	$4 \mathbb{G}  +  \mathbb{Z}_p $	$[0,0,5,1]$	$[3,0,2,0]$	<b>SXDH</b>

$r$  : randomness that depends on the security parameter

$n$  : size of ID space (i.e.,  $I := \{0,1\}^n$ )

# CCA-secure Hierarchical IKE

An well-known transformation [CHK04,BCHK06] :



We cannot apply the transformation to a hierarchical IKE scheme in a generic way since it does not have delegating functionality:



However, by modifying the proposed hierarchical IKE scheme, we can realize CCA-secure scheme based on the transformation:





# Conclusion

**We proposed  $\ell$ -level hierarchical IKE scheme:**

- met strong security (IND-KE-CPA security) without ROM
- secure under the SXDH assumption, which is a simple, static one
- achieved constant-size parameters when  $\ell = 1$

**We also showed CCA-secure scheme from**

- Proposed CPA-secure hierarchical IKE scheme; and
- Any one-time signature

